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Det: Medicine and surgery.

1.  $\int \sin^6 x \, dx$

solution

$$\int \sin^6 x \, dx = \int (\sin^2 x)^3 \, dx$$
$$= \int \left[ \frac{1 - 2\cos 2x}{2} \right]^3 \, dx$$

$$= \frac{1}{8} \int (1 - 2\cos 2x)^3 \, dx = \frac{1}{8} \int (1 - 2\cos 2x)^2 (1 - 2\cos 2x) \, dx$$

$$= \frac{1}{8} \int (1 - 4\cos 2x + 4\cos^2 2x) (1 - 2\cos 2x) \, dx$$

$$= \frac{1}{8} \int (1 - 6\cos 2x + 12\cos^2 2x - 8\cos^3 2x) \, dx$$

$$= \frac{1}{8} \int \left[ 1 - 6\cos 2x + 12 \left( \frac{1 + \cos 4x}{2} \right) - 8\cos^2 2x \right] \, dx$$

$$= \frac{1}{8} \left[ \int dx - 6 \int (1 + \cos 4x) \, dx - 8 \int \cos^2 2x \, dx \right]$$

and  $\int \cos^3 2x \, dx = \int \cos^2 2x \cdot \cos 2x \, dx$

$$= \int \frac{\cos 2x (1 + \cos 4x)}{2} \, dx$$

$$\begin{aligned}
 \int \cos^4 x \sin^3 x \, dx &= \int \cos^4 x \sin^2 x \sin x \, dx \\
 &= \int \cos^4 x (1 - \cos^2 x) \sin x \, dx \\
 &= \int u^4 (1 - u^2) \left(-\frac{du}{\sin x}\right) \\
 &= -\int u^4 (1 - u^2) \, du \\
 &= -\int (u^4 - u^6) \, du \\
 &= -\left[\frac{u^5}{5} - \frac{u^7}{7}\right] + C \\
 &= -\frac{u^5}{5} + \frac{u^7}{7} + C
 \end{aligned}$$

$$\therefore \int \cos^4 x \sin^3 x \, dx = \frac{\cos^7 x}{7} - \frac{\cos^5 x}{5} + C$$

3.  $\int \cos x \sin^3 x \, dx$

Solution

$$\begin{aligned}
 \int \cos x \sin^3 x \, dx &= \int \cos x \sin^2 x (1 - \cos^2 x) \left(-\frac{du}{\sin x}\right) \\
 &= -\int u (1 - u^2) \, du \\
 &= -\int (u - u^3) \, du = \int (u^3 - u) \, du \\
 &= \frac{u^4}{4} - \frac{u^2}{2} + C
 \end{aligned}$$

$$\therefore \int \cos x \sin^3 x \, dx = \frac{\cos^4 x}{4} - \frac{\cos^2 x}{2} + C$$

$$\int \cos x \sin^3 x \, dx = \frac{\cos^4 x}{4} - \frac{\cos^2 x}{2} + C$$